

CMSC427 Fall 2017
Hw 3 – Vectors

Due by 5 pm on Friday, Sept. 25th
On Elms as a pdf

1. Warm up. Is the angle between $\langle 2, 3, 2 \rangle$ and $\langle -3, 1, 2 \rangle$ obtuse or acute?
2. For what values of α is \mathbf{a} orthogonal to $\mathbf{b} - \alpha\mathbf{a}$? What about the special case where $\|\mathbf{a}\| = 1$? The case where $\|\mathbf{a}\| = 0$?
3. Given a helix curve in parametric vector form as $\mathbf{P}(t) = \langle r\cos(t), h*t, r\sin(t) \rangle$, what is the tangent vector \mathbf{T} to the curve? What is the normal vector \mathbf{N} (which is \mathbf{T}')? And what is the binormal vector \mathbf{B} (which is $\mathbf{T} \times \mathbf{N}$)?
4. For the previous problem the appropriate range of t isn't important – for actually drawing a helix, picking the range of t to appropriate scale h and the number of twists is important. Redo the helix equation so as t goes from 0 to 1, the helix makes N full turns and rises to a height h .
5. For the lecture example for the midpoint of a triangle, calculated by first blending the line segment between two points P_0 and P_1 , and then blending that equation with the third point P_2 , show that (a) if you hold s constant then varying t sweeps out a line, and (b) those lines of constant s are parallel to the line from P_0 to P_1 .
6. If you have $\mathbf{a} \cdot (\mathbf{b} \times \mathbf{c}) = 0$, what does it mean for the relationship of the three vectors?
7. Find the normal vector to the triplets below, if it exists:
 - a) $P_1=(1,1,1), P_2=(1,2,1), P_3=(3,0,4)$
 - b) $P_1=(8,16,2), P_2=(-8,-16,-2), P_3=(4,8,1)$