

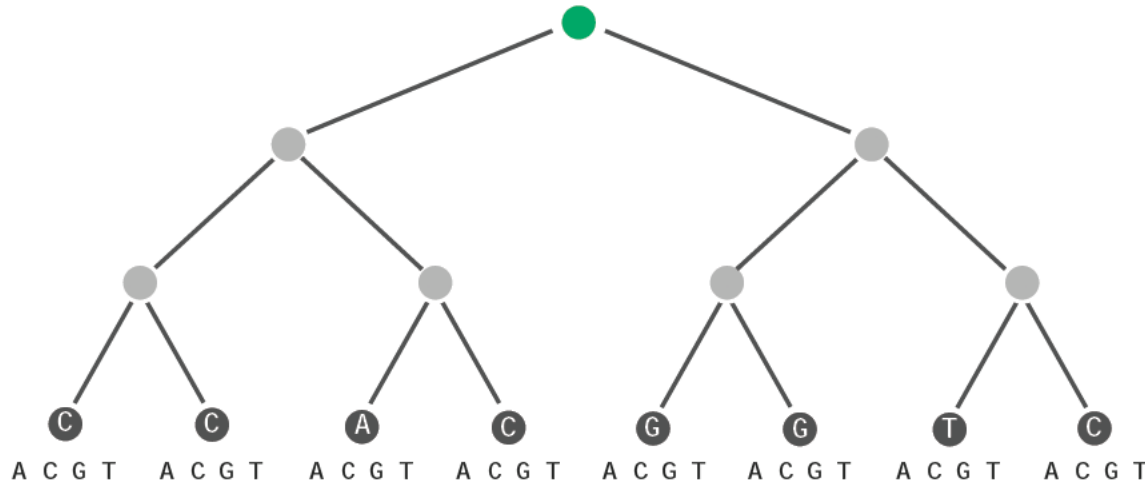
Sankoff's algorithm – recurrence relation

- Traverse the tree in post-order and update $s(v,t)$ as follows
 - assume node v has children u and w
 - $s(v,t) = \min_i \{s(u,i) + \text{score}(i,t)\} + \min_j \{s(w,j) + \text{score}(j,t)\}$
- the minimum parsimony score is given by the smallest score $s(\text{root},t)$ over all symbols t
- backtrack to fill the values for the other nodes
- Note – this solves the weighted version. For unweighted set $\text{score}(i,i) = 0$, $\text{score}(i,j) = 1$ for any i,j

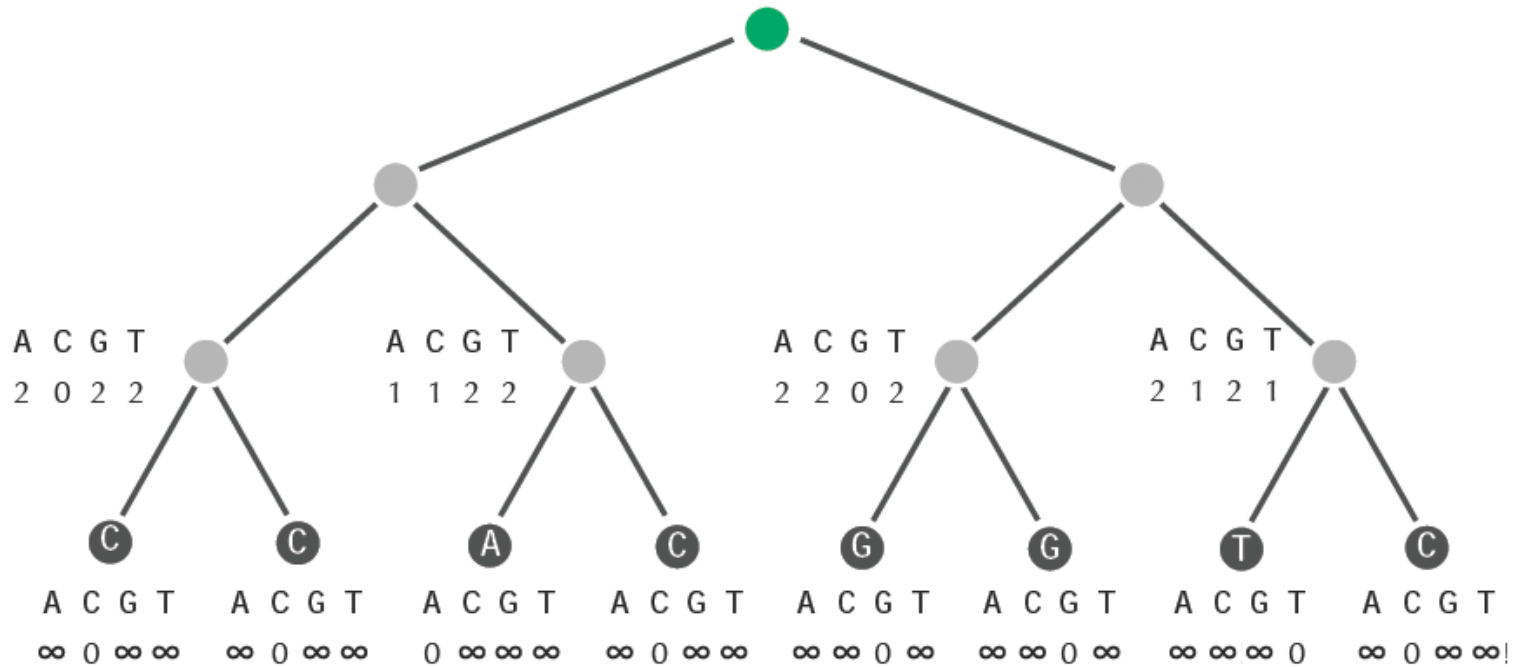
Sankoff's algorithm – recurrence relation

- At each node v in the tree store $s(v,t)$ – best parsimony score for subtree rooted at v if character stored at v is t

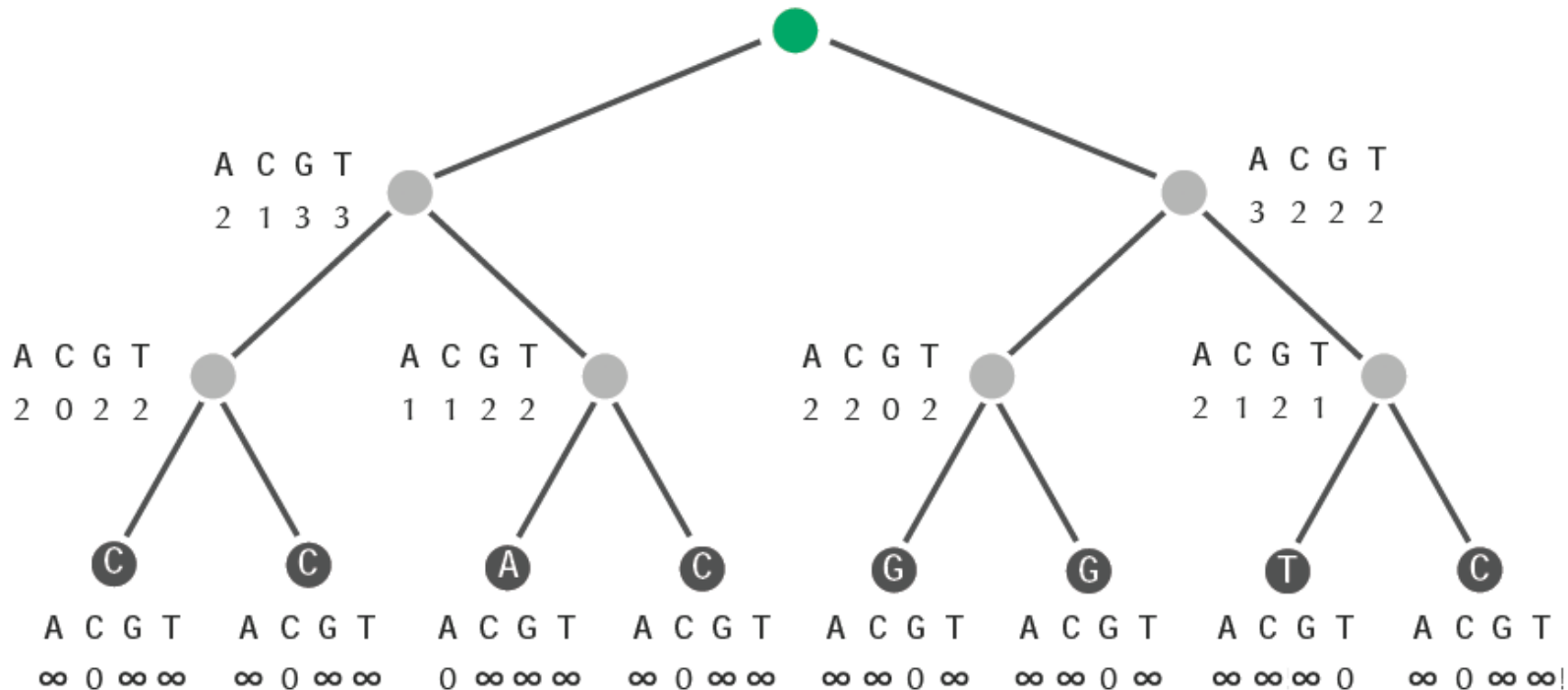
What is the base case?



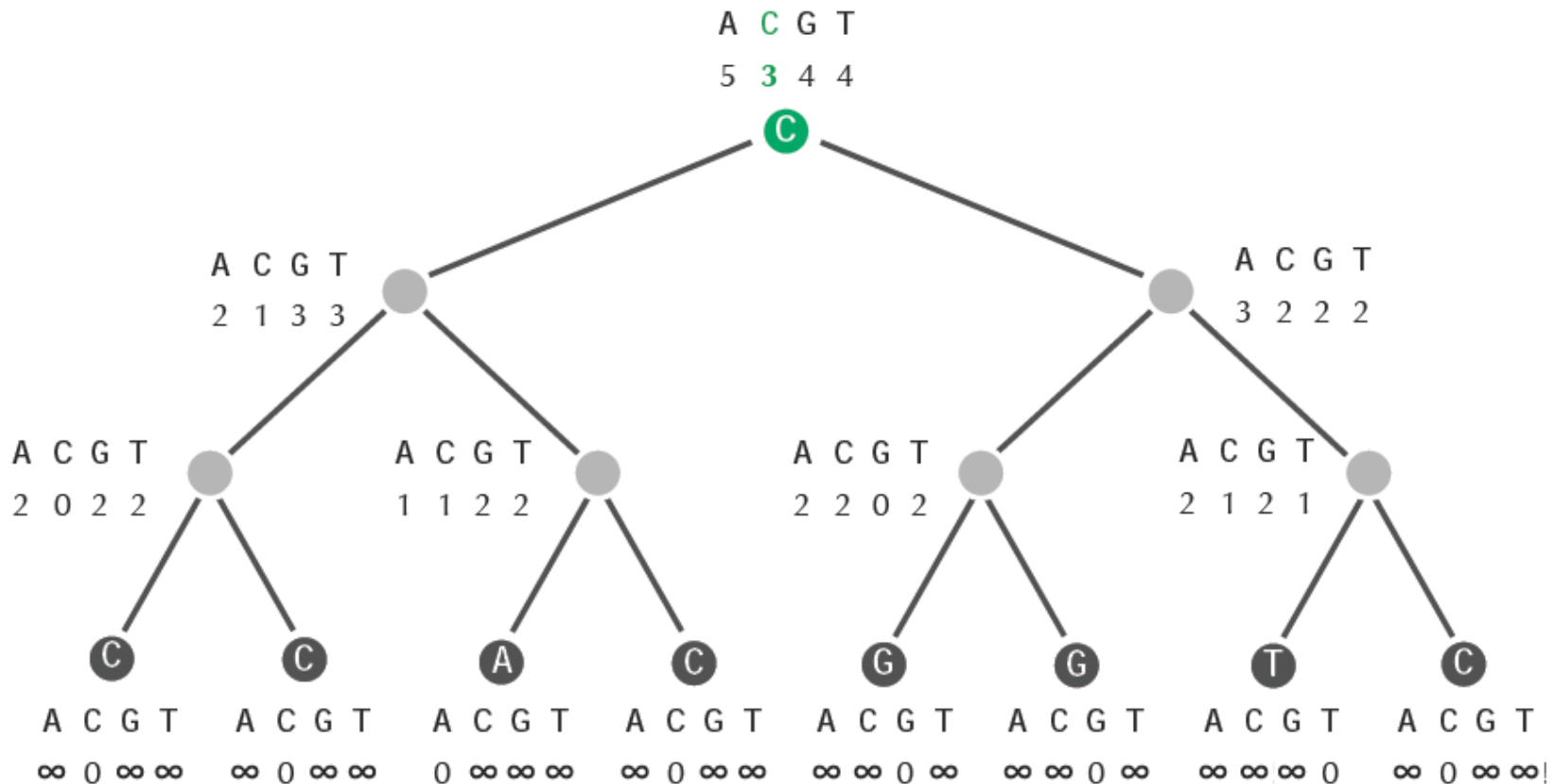
Sankoff's algorithm – example (continued)



Sankoff's algorithm – example (continued)



Sankoff's algorithm – example (continued)



Optimal labeling can be computed in linear time $O(nk)$ where n is number of leaves and k is number of character states